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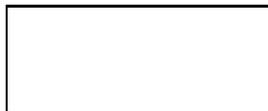
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Problem 3. Eight points are located in the plane. How many ways can you draw four line segments, each starting at one of the points and ending at another, if you must use each point exactly once?



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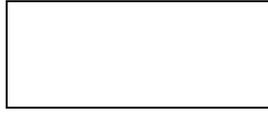
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